$\qquad$ Date $\qquad$
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## 6-7 <br> Investigating Graphs of Polynomial Functions

Identify the leading coefficient, degree, and end behavior.

1. $P(x)=2 x^{5}-6 x^{3}+x^{2}-2$
2. $Q(x)=-4 x^{2}+x-1$

Identify whether the function graphed has an odd or even degree and a positive or negative leading coefficient.
3.

4.

5.


Graph the function $P(x)=x^{3}+6 x^{2}+5 x-12$.
6. Identify the possible rational roots.
7. Identify the zeros.
8. Describe the end behavior of the function.
9. Sketch the graph of the function.


Solve.
10. The number, $N(y)$, of subscribers to a local magazine can be modeled by the function $N(y)=0.1 y^{4}-3 y^{3}+10 y^{2}-30 y+10,000$, where $y$ is the number of years since the magazine was founded. Graph the polynomial on a graphing calculator and find the minimum number of subscribers and the year in which this occurs.
negative, so they cannot be the radius.
7. 0.5 inch

## Reading Strategies

1. Find the factors corresponding to the roots and multiply the factors.
2. $x$
3. a. $(x+2)(x+2)(x+2)=0$, or $x^{3}+6 x^{2}+$ $12 x+8$
b. because multiplying the equation by a nonzero number will not change its roots
4. a. $(x)(x)(x)(x+2)=x^{4}+2 x^{3}=0$ b. 4

## LESSON 6-7

## Practice A

1. $1 ; 2$
2. $-3 ; 3$
3. $2 ; 4 ; x \rightarrow-\infty, P(x) \rightarrow+\infty ; x \rightarrow+\infty$,

$$
P(x) \rightarrow+\infty
$$

4. $-6 ; 5 ; x \rightarrow-\infty, P(x) \rightarrow+\infty ; x \rightarrow+\infty$,

$$
P(x) \rightarrow-\infty
$$

5. $\pm 1, \pm 2, \pm 4$
6. $(x-1)\left(x^{2}+5 x+4\right)$
7. $(x-1)(x+4)(x+1)$
8. $y$-intercept $=-4 ; P(-2)=6 ; P(-3)=8$
9. As $x \rightarrow-\infty, P(x) \rightarrow-\infty$, as $x \rightarrow+\infty$, $P(x) \rightarrow+\infty$
10. 



## Practice B

1. 2; 5; as $x \rightarrow+\infty, P(x) \rightarrow+\infty$; and as

$$
x \rightarrow-\infty, P(x) \rightarrow-\infty
$$

2. -4 ; 2; as $x \rightarrow-\infty, Q(x) \rightarrow-\infty$; and as

$$
x \rightarrow+\infty, Q(x) \rightarrow-\infty
$$

3. Even; negative
4. Even; positive
5. Odd; positive
6. $\pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12$
7. $-4,-3$, and 1
8. As $x \rightarrow+\infty, P(x) \rightarrow+\infty$, and as $x \rightarrow-\infty$, $P(x) \rightarrow-\infty$
9. 


10. About 5400 in year 20

## Practice C

1. -6 ; 4; as $x \rightarrow-\infty, R(x) \rightarrow-\infty$ : and as $x \rightarrow+\infty, R(x) \rightarrow-\infty$
2. -16 ; 3; as $x \rightarrow-\infty, Q(x) \rightarrow+\infty$ : and as $x \rightarrow+\infty, Q(x) \rightarrow-\infty$
3. Odd; negative
4. Even; positive
5. Odd; positive
6. 


7. Minima: 4.5; maxima: 5.1 and 13.5
8. Minima: -8.68; maxima: 0
9. a. $3.03 \mathrm{~m}^{3}$
b. 1.9 m by 2.9 m by 0.55 m

