20 1<del>6</del> 12

8

2 0

4

8

16 20 2

10 -8 -6

LESSON Practice B

Investigating Graphs of Polynomial Functions

Identify the leading coefficient, degree, and end behavior.

1. 
$$P(x) = 2x^5 - 6x^3 + x^2 - 2$$

2. 
$$Q(x) = -4x^2 + x - 1$$

# Identify whether the function graphed has an odd or even degree and a positive or negative leading coefficient.



Graph the function  $P(x) = x^3 + 6x^2 + 5x - 12$ .

- 6. Identify the possible rational roots.
- 7. Identify the zeros.
- 8. Describe the end behavior of the function.

9. Sketch the graph of the function.

# Solve.

10. The number, N(y), of subscribers to a local magazine can be modeled by the function  $N(y) = 0.1y^4 - 3y^3 + 10y^2 - 30y + 10,000$ , where *y* is the number of years since the magazine was founded. Graph the polynomial on a graphing calculator and find the minimum number of subscribers and the year in which this occurs.

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negative, so they cannot be the radius.

7. 0.5 inch

#### **Reading Strategies**

- 1. Find the factors corresponding to the roots and multiply the factors.
- 2. *x*
- 3. a. (x + 2)(x + 2)(x + 2) = 0, or  $x^3 + 6x^2 + 12x + 8$ .
  - b. because multiplying the equation by a nonzero number will not change its roots
- 4. a.  $(x)(x)(x)(x+2) = x^4 + 2x^3 = 0$ b. 4

# **LESSON 6-7**

#### **Practice A**

- 1. 1; 2 2. –3; 3
- 3. 2; 4;  $x \to -\infty$ ,  $P(x) \to +\infty$ ;  $x \to +\infty$ ,  $P(x) \to +\infty$
- 4. -6; 5;  $x \to -\infty$ ,  $P(x) \to +\infty$ ;  $x \to +\infty$ ,  $P(x) \to -\infty$
- 5. ±1, ±2, ±4
- 6.  $(x-1)(x^2+5x+4)$

7. 
$$(x-1)(x+4)(x+1)$$

- 8. *y*-intercept = -4; P(-2) = 6; P(-3) = 8
- 9. As  $x \to -\infty$ ,  $P(x) \to -\infty$ , as  $x \to +\infty$ ,  $P(x) \to +\infty$



#### **Practice B**

- 1. 2; 5; as  $x \to +\infty$ ,  $P(x) \to +\infty$ ; and as  $x \to -\infty$ ,  $P(x) \to -\infty$
- 2. -4; 2; as  $x \to -\infty$ ,  $Q(x) \to -\infty$ ; and as

- $x \to +\infty, Q(x) \to -\infty$
- 3. Even; negative 4. Even; positive
- 5. Odd; positive
- 6.  $\pm 1$ ,  $\pm 2$ ,  $\pm 3$ ,  $\pm 4$ ,  $\pm 6$ ,  $\pm 12$
- 7. -4, -3, and 1
- 8. As  $x \to +\infty$ ,  $P(x) \to +\infty$ , and as  $x \to -\infty$ ,  $P(x) \to -\infty$



10. About 5400 in year 20

# Practice C

- 1. -6; 4; as  $x \to -\infty$ ,  $R(x) \to -\infty$ : and as  $x \to +\infty$ ,  $R(x) \to -\infty$
- 2. -16; 3; as  $x \to -\infty$ ,  $Q(x) \to +\infty$ : and as  $x \to +\infty$ ,  $Q(x) \to -\infty$
- 3. Odd; negative 4. Even; positive
- 5. Odd; positive



- 7. Minima: 4.5; maxima: 5.1 and 13.5
- 8. Minima: -8.68; maxima: 0
- 9. a. 3.03 m<sup>3</sup>
  - b. 1.9 m by 2.9 m by 0.55 m

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