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## 8-8 Solving Radical Equations and Inequalities

## Solve each equation.

1. $\sqrt{x+6}=7$
2. $\sqrt{5 x}=10$
3. $\sqrt{2 x+5}=\sqrt{3 x-1}$
4. $\sqrt{x+4}=3 \sqrt{x}$
5. $\sqrt[3]{x-6}=\sqrt[3]{3 x+24}$
6. $3 \sqrt[3]{x}=\sqrt[3]{7 x+5}$
7. $\sqrt{-14 x+2}=x-3$
8. $(x+4)^{\frac{1}{2}}=6$
9. $4(x-3)^{\frac{1}{2}}=8$
10. $4(x-12)^{\frac{1}{3}}=-16$
$\qquad$
Solve each inequality.
11. $\sqrt{3 x+6} \leq 3$
12. $\sqrt{x-4}+3>9$
13. $\sqrt{x+7} \geq \sqrt{2 x-1}$
14. $\sqrt{2 x-7}>9$

Solve.
15. A biologist is studying two species of animals in a habitat. The population, $p_{1}$, of one of the species is growing according to $p_{1}=500 t^{\frac{3}{2}}$ and the population, $p_{2}$, of the other species is growing according to $p_{2}=100 t^{2}$ where time, $t$, is measured in years. After how many years will the populations of the two species be equal?

## Practice B

1. $x=43$
2. $x=20$
3. $x=6$
4. $x=\frac{1}{2}$
5. $x=-15$
6. $x=\frac{1}{4}$
7. No solutions, since both -1 and -7 are extraneous
8. $x=32$
9. $x=7$
10. $x=-52$
11. $-2 \leq x \leq 1$
12. $x>40$
13. $\frac{1}{2} \leq x \leq 8$
14. $x>44$
15. 25 years

## Practice C

1. $x=31$
2. $x=47$
3. $x=7$
4. $x=9$
5. $x=-2$ and $x=1$
6. $x=5$
7. $x=\frac{5}{2}$
8. $x=9 ; x=-2$ is an extraneous solution.
9. $-\frac{5}{4} \leq x \leq 1$
10. $x \geq 5$
11. $7 \leq x \leq 16$
12. $x>-21$
13. $x>4$
14. $-2 \leq x \leq 123$
15. $v=\frac{\sqrt{3}}{2} c$

## Reteach

1. $2 x+11=27$
$2 x=16 ; x=8$
$4 \sqrt[3]{2(8)+11}=12$
$4 \sqrt[3]{36}=12 \checkmark$
2. $\sqrt{x-3}=4$
$x-3=16$
$x=19$
$5+\sqrt{19-3}=5$
$5+\sqrt{16}=5+4$
$=9 \checkmark$
3. 7
4. 6

## Problem Solving

1. Directly
2. a. $d=\frac{s^{2}}{30 f}$
b. About 58 ft
c. No; possible answer: his skid marks were only 52 ft , not 58 ft .
d. About $33 \mathrm{mi} / \mathrm{h}$
3. a. About 9 ft
b. By at least 15 ft
4. B
5. A
6. $\sqrt{x+4}=5$
$x+4=25$
$x=21$
$2 \sqrt{21+4}=$
$2 \sqrt{25}=2 \cdot 5$
$=10 \checkmark$
7. $5 x+6=81$
$5 x=75$
$x=15$
8. $\left[(6 x-8)^{\frac{1}{3}}\right]^{3}=4^{3}$
$6 x-8=64$
$6 x=72$
$x=12$
9. $x^{2}=\left[(x+6)^{\frac{1}{2}}\right]^{2}$
$x^{2}=x+6$
$x^{2}-x-6=0$
$(x-3)(x+2)=0$
$x=3$

## Challenge

1. 15.25
2. 9
3. No solution
4. 19
5. 5
6. 3
7. 5 or $-\frac{1}{9}$
8. 8 or -1
