

1. Identify all of the roots of the equation by factoring, using the Rational Root Theorem and synthetic division to find a depressed polynomial that can be solved by using the quadratic formula. State the multiplicity of each root, if more than one.

a. $x^4 - 36 = 0$

b. $x^3 - 8 = 0$

c. $x^4 - 6x^3 = -9x^2$

d. $x^3 - 5x^2 - 4x + 20 = 0$

2. Solve by finding all roots by using the calculator to find as many rational roots as possible, then use synthetic division and the quadratic formula to find the remaining roots. Show all work!

$x^4 - 5x^3 - 2x^2 - 20x - 24 = 0$

3. Write factors of the simplest polynomial function with rational coefficients that has the given zeros, then multiply out the factors to give the polynomial function in standard form.

a. 5, 1, -1

a. factors: _____

polynomial function: $f(x) =$ _____

b. 1, $5i$

b. factors: _____

polynomial function: $f(x) =$ _____

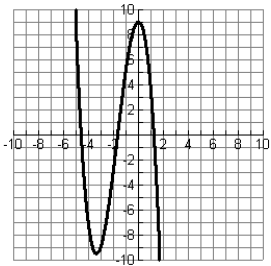
c. -3, $-\sqrt{2}$

c. factors: _____

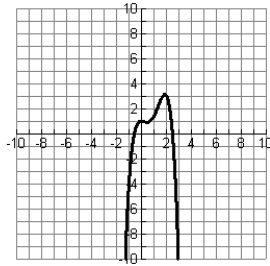
polynomial function: $f(x) =$ _____

Classify each of the graphs of the polynomial functions below by their degree and leading coefficient. Then determine the end behavior of each graph.

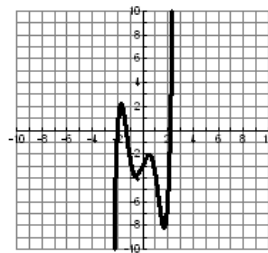
4.



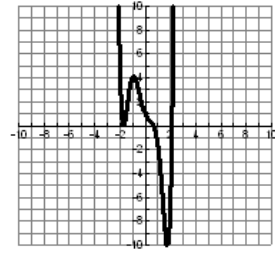
5.



6.



7.



Circle the correct choice.

Degree: Even or OddDegree: Even or OddDegree: Even or OddDegree: Even or OddLeading Coefficient is Positive or NegativeLeading Coefficient is Positive or NegativeLeading Coefficient is Positive or NegativeLeading Coefficient is Positive or NegativeAs $x \rightarrow -\infty$, $f(x) \rightarrow$ ___As $x \rightarrow -\infty$, $f(x) \rightarrow$ ___As $x \rightarrow -\infty$, $f(x) \rightarrow$ ___As $x \rightarrow -\infty$, $f(x) \rightarrow$ ___As $x \rightarrow +\infty$, $f(x) \rightarrow$ ___As $x \rightarrow +\infty$, $f(x) \rightarrow$ ___As $x \rightarrow +\infty$, $f(x) \rightarrow$ ___As $x \rightarrow +\infty$, $f(x) \rightarrow$ ___

Match the polynomial equation with its end behavior.

8. ___ $f(x) = 4x^3 + 5x^2 + 1$

A. As $x \rightarrow -\infty$, $f(x) \rightarrow -\infty$
As $x \rightarrow +\infty$, $f(x) \rightarrow -\infty$

9. ___ $f(x) = 2x^4 - 5x + 3$

B. As $x \rightarrow -\infty$, $f(x) \rightarrow +\infty$
As $x \rightarrow +\infty$, $f(x) \rightarrow -\infty$

10. ___ $f(x) = -2x^3 + x - 5$

C. As $x \rightarrow -\infty$, $f(x) \rightarrow +\infty$
As $x \rightarrow +\infty$, $f(x) \rightarrow +\infty$

11. ___ $f(x) = -3x^4 - 7x^2 + 1$

D. As $x \rightarrow -\infty$, $f(x) \rightarrow -\infty$
As $x \rightarrow +\infty$, $f(x) \rightarrow +\infty$

12. Solve each polynomial equation by factoring.

a. $x^3 - x^2 - 9x + 9 = 0$

b. $x^4 - 11x^2 + 28 = 0$

c. $x^4 - 6x^3 + 9x^2 = 0$

13. Use the Rational Root Theorem to list all the possible rational roots of the polynomial equation.

$7x^3 + 6x^2 - 4x - 6 = 0$

14. Use your graphing calculator to estimate the real zeros, local maximum, and local minimum of $f(x) = x^3 - 10x + 1$. Round your answers to the nearest thousandth.

real zeros _____, _____, _____ maximum _____ minimum _____

15. Which polynomial function with rational coefficients has zeros $1 + \sqrt{5}$ and $1 - \sqrt{5}$?

A. $f(x) = x^2 + 2x - 4$ B. $f(x) = x^2 - 2x - 4$ C. $f(x) = x^2 + 4$ D. $f(x) = x^2 - 3x - 6$

16. A polynomial function of degree n has at most _____ turning points (local maxima and local minima) and at most _____ x-intercepts.

17. In each box, sketch a graph of a polynomial function that fits the description.

Leading coefficient	Odd degree	Even degree
Positive		
Negative		

18. Determine the best Polynomial Function for the given data using Finite Differences and give the r^2 value.

Time	2	4	6	8	10	12	14	16	18
Velocity	24.51	16.44	-8.91	-59.70	-142.56	-262.57	-423.28	-626.71	-873.34